

Normal Practice 2 Continued:

6. Given $N(420, 3.4)$

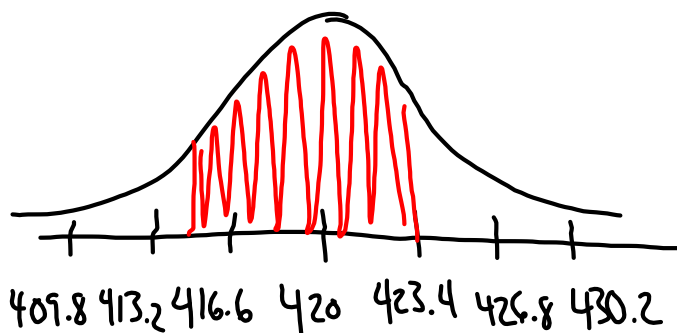
Left cutpoint = 415

Right z-score = 1

$$\text{Left } z = \frac{y - \mu}{\sigma} = \frac{415 - 420}{3.4} = -1.47$$

Right cutpoint:

$$\begin{aligned} y &= z\sigma + \mu \\ &= (1)(3.4) + 420 \\ &= 423.4 \end{aligned}$$



find percentage:

$$\text{normalcdf}(-1.47, 1) = .77 = 77\%$$

Example:

Given: Center 95%

Left cutpoint = 10

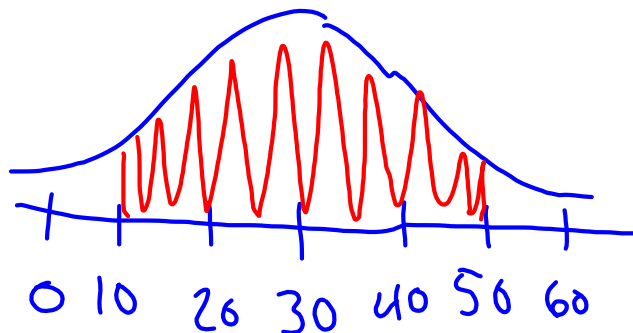
Right cutpoint = 50

Find: $N(-, -)$, σ , z -scores

Center 95% $\rightarrow \pm 2\sigma$

$$z_L = -2 \quad c_L = 10$$

$$z_R = 2 \quad c_R = 50$$



$$\mu = \frac{50 + 10}{2} = 30 \quad \sigma = 10$$

$$N(30, 10)$$

Example:

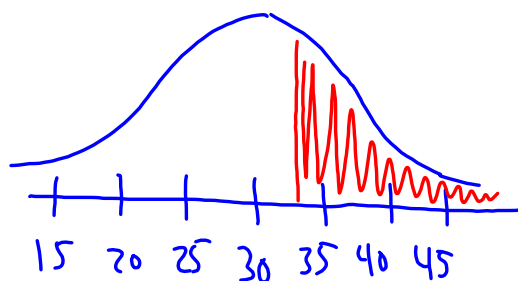
Given: Highest 25%

$$N(30, 5)$$

Find: Left and right cutpoints

Left and right z-scores

Shading



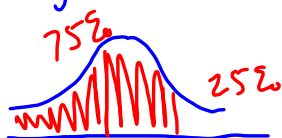
$$C_R = +\infty$$

$$z_R = +\infty$$

$$z_L = \text{invNorm}(0.75) = 0.67$$

↑
always a decimal

* invNorm goes from $-\infty$ to a cutpoint



$$\begin{aligned} C_L: \quad y &= z\sigma + \mu \\ &= (0.67)(5) + 30 \\ &= 33.4 \end{aligned}$$

Review:

Unimodal, symmetric distribution →

one peak, halves of distribution are mirror images of each other.

Standard Deviation →

measure of spread of data based on distance from the mean

Using the standard deviation as a ruler →

By measuring in standard deviations, we can compare values from distributions that have different scales

Z-score →

measure of how many standard deviations value is from mean

$$Z = \frac{Y - M}{\sigma} \quad (\text{for normal model})$$

Normal Model →

Useful model for describing unimodal, symmetrical distributions

68-95-99.7 Rule →

68 → $\pm 1\sigma$ percent
 95 → $\pm 2\sigma$ of
 99.7 → $\pm 3\sigma$ information

Calculator:

2nd VARS → 2: normalcdf(Z_L, Z_R)
 (DISTR)
 → 3: invNorm(percent from left)
 answer is z-score